

# Validating NEUTRO: a deterministic neutron transport solver for fusion applications

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CONICET

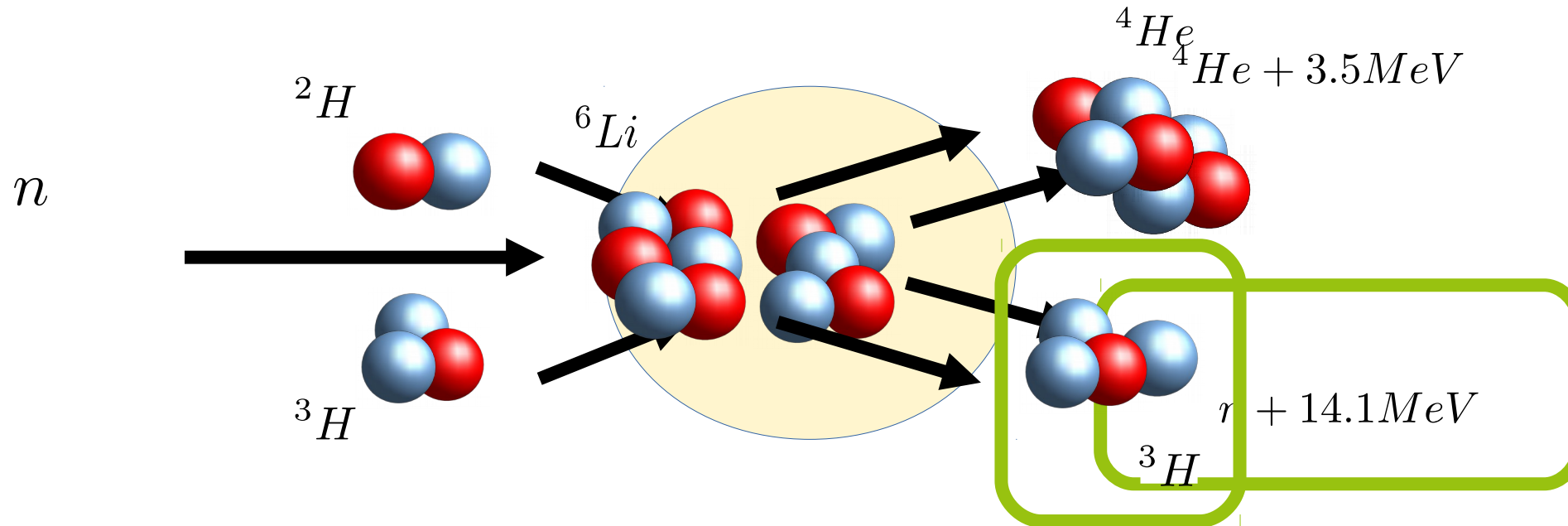


# Outline

- ☀️ Background
- ☀️ NEUTRO
- ☀️ Results
- ☀️ HPC scalability
- ☀️ Ongoing and future work
- ☀️ Conclusions

# Background

- ☀ Nuclear Fusion: D-T reaction produces high-energy neutrons.
- ☀ Tritium production (Breeding Blanket)



# Background

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## NEUTRO

Neutron transport solver coupled within Alya multiphysics framework to study:

- ☀️ Shielding.
- ☀️ Tritium production (Breeding Blanket).
- ☀️ Heat
- ☀️ Damage

- ☀️ Deterministic
  - ☀️ Less computationally intensive than statistical methods.
  - ☀️ Global analysis.
  - ☀️ Complements other approaches such as Monte Carlo.

# NEUTRO

☀️ Aims to solve the stationary Boltzmann neutron transport equation:

$$\underbrace{\hat{\Omega} \cdot \nabla \varphi}_{\text{Leakage}} + \underbrace{\Sigma_t(\mathbf{r}, E, \hat{\Omega}) \varphi}_{\text{Collision}} = \underbrace{\int_0^\infty \int_{4\pi} \Sigma_s(\mathbf{r}, E' \rightarrow E, \hat{\Omega}' \rightarrow \hat{\Omega}) \varphi d\hat{\Omega}' dE'}_{\text{In-scattering}} + \underbrace{s(\mathbf{r}, E, \hat{\Omega})}_{\text{Source}}$$

Loss terms Gain terms

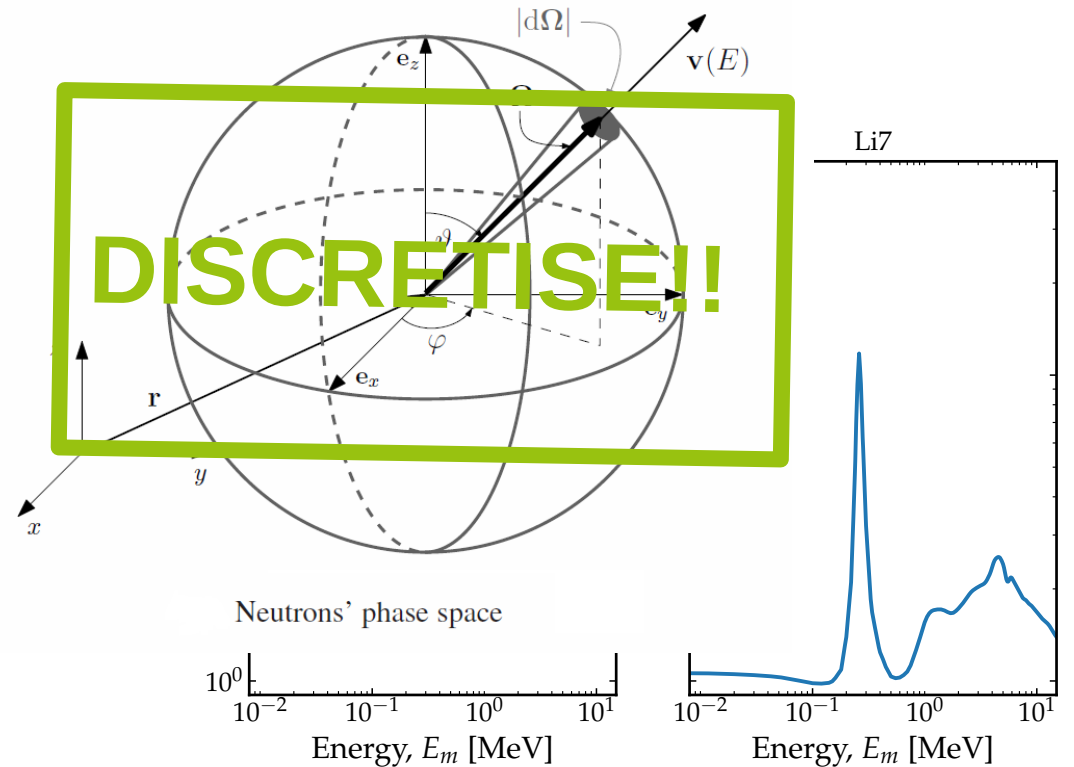
# NEUTRO

$$\hat{\Omega} \cdot \nabla \varphi + \Sigma_t(\mathbf{r}, E, \hat{\Omega}) \varphi = \int_0^\infty \int_{4\pi} \Sigma_s(\mathbf{r}, E' \rightarrow E, \hat{\Omega}' \rightarrow \hat{\Omega}) \varphi d\hat{\Omega}' dE' + s(\mathbf{r}, E, \hat{\Omega})$$

Where:

- $\hat{\Omega}$  : neutron's direction of flight.
- $E$  : neutron's energy.
- $\mathbf{r}$  : spatial variable.
- $\varphi$  : distribution function of neutrons in  $\mathbf{r}, E, \hat{\Omega}$ .

- $\Sigma_t$  : total macroscopic cross-section.
- $\Sigma_s$  : scattering macroscopic cross-section.
- $s$  : external neutron source.

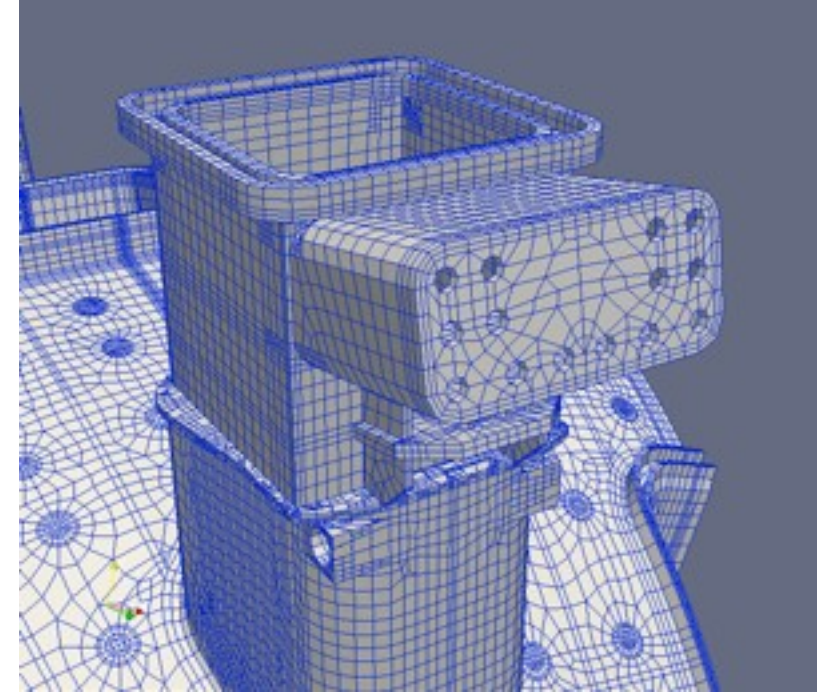


# NEUTRO: Finite Element Method

- ☀️ Spatial variable,  $r$ , is discretised using FEM.
- ☀️ Spatial meshes of a fusion reactor can easily reach  $\sim 10^9$  elements.
- ☀️ NEUTRO software is include within the **Alya** ecosystem.

## Alya

- ☀️ Solves partial differential equations (PDEs) in non-structured meshes.
- ☀️ Designed for supercomputers (MareNostrum).
- ☀️ Excellent scalability proven up to 100k processors.
- ☀️ Implements parallel frameworks at different levels without user active intervention.
- ☀️ Solves coupled multiphysics problems.



# NEUTRO: Multigroup Approximation

- ☀ Discretise the energy continuum into  $G$  energy groups:  $E_1, E_2, \dots, E_{G-1}, E_G$
- ☀ Properties of neutrons and materials remain constant within each interval of energy.

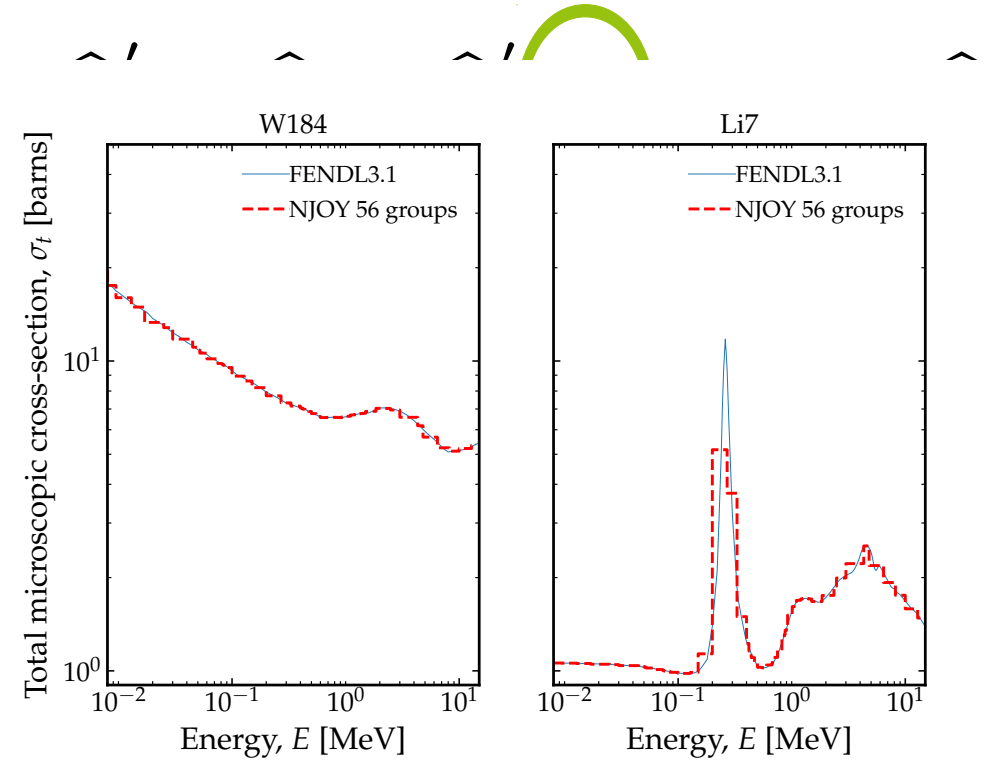
$$\hat{\Omega} \cdot \nabla \varphi + \Sigma_t(\mathbf{r}, E, \hat{\Omega}) \varphi = \int_0^\infty \int_{4\pi} \Sigma_s(\mathbf{r}, E' \rightarrow E, \hat{\Omega}') \varphi(\mathbf{r}, E', \hat{\Omega}') d\Omega' dE'$$

$$\Sigma_{t,g}(\mathbf{r}, \hat{\Omega}) \varphi_g = \sum_{g'=0}^G \int_{4\pi} \Sigma_{s,g',g}(\mathbf{r}, \hat{\Omega}') \varphi_{g'}(\mathbf{r}, \hat{\Omega}') d\Omega'$$

Evaluated Nuclear Data Files (ENDF)



NJOY

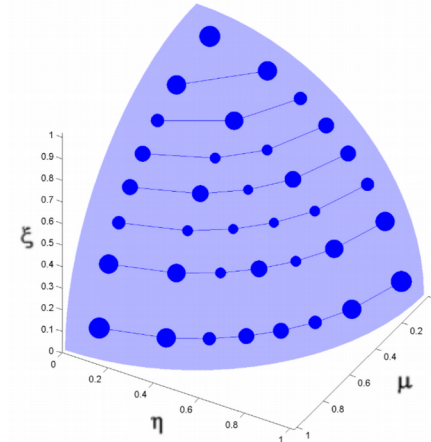




# NEUTRO: Angular discretisation

- ☀ Discrete Ordinates Methods ( $S_N$ ): equal-level set
- ☀ Divide neutron's phase space in quadrature points with adequate weights.

$$\hat{\Omega} \cdot \nabla \varphi_g + \Sigma_{t_g}(\mathbf{r}, \hat{\Omega}) \varphi_g = \sum_{g'=0}^G \int_{4\pi} \Sigma_{s_{g',g}}(\mathbf{r}, \hat{\Omega}' \rightarrow \hat{\Omega}) \varphi_{g'} d\hat{\Omega}' + s_g(\mathbf{r}, \hat{\Omega})$$



$$\Omega_m \cdot \nabla \varphi_g + \Sigma_{t_{gm}}(\mathbf{r}) \varphi_{gm} = \sum_{g'=0}^G \sum_{m'=0}^M \Sigma_{s_{g',gm',m}}(\mathbf{r}) \varphi_{g'm'} + s_{gm}(\mathbf{r})$$

# NEUTRO: Material anisotropy

☀ Introduced in  $\Sigma_s$  using real-based spherical harmonics.

☀  $L > 0 \rightarrow$  angular anisotropy.

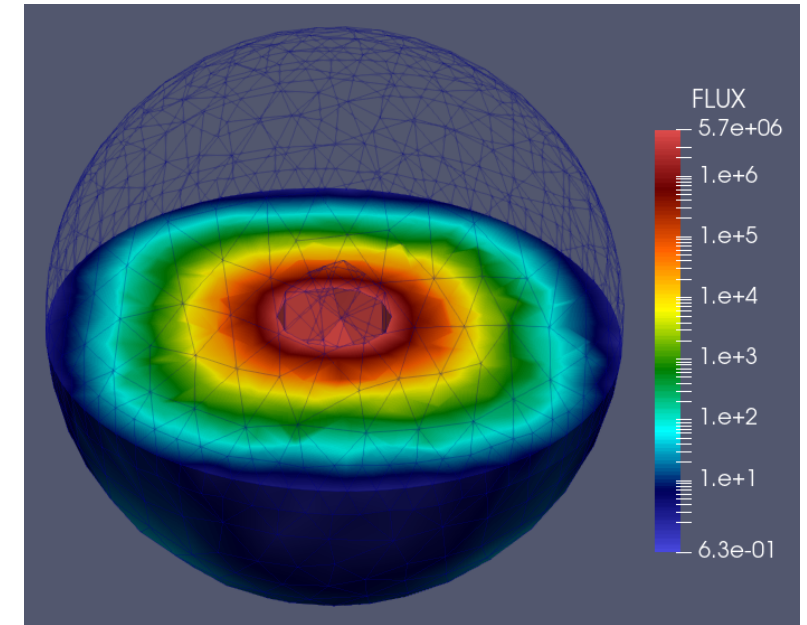
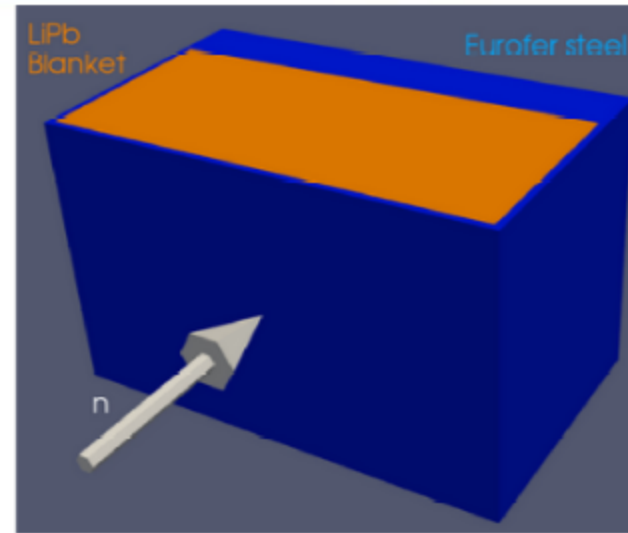
$$\Omega_m \cdot \nabla \varphi_g + \Sigma_{t_{gm}}(\mathbf{r}) \varphi_{gm} = \sum_{g'=0}^G \sum_{m'=0}^M \underbrace{\Sigma_{s_{g',gm',m}}(\mathbf{r}) \varphi_{g'm'}}_{\text{anisotropy}} + s_{gm}(\mathbf{r})$$



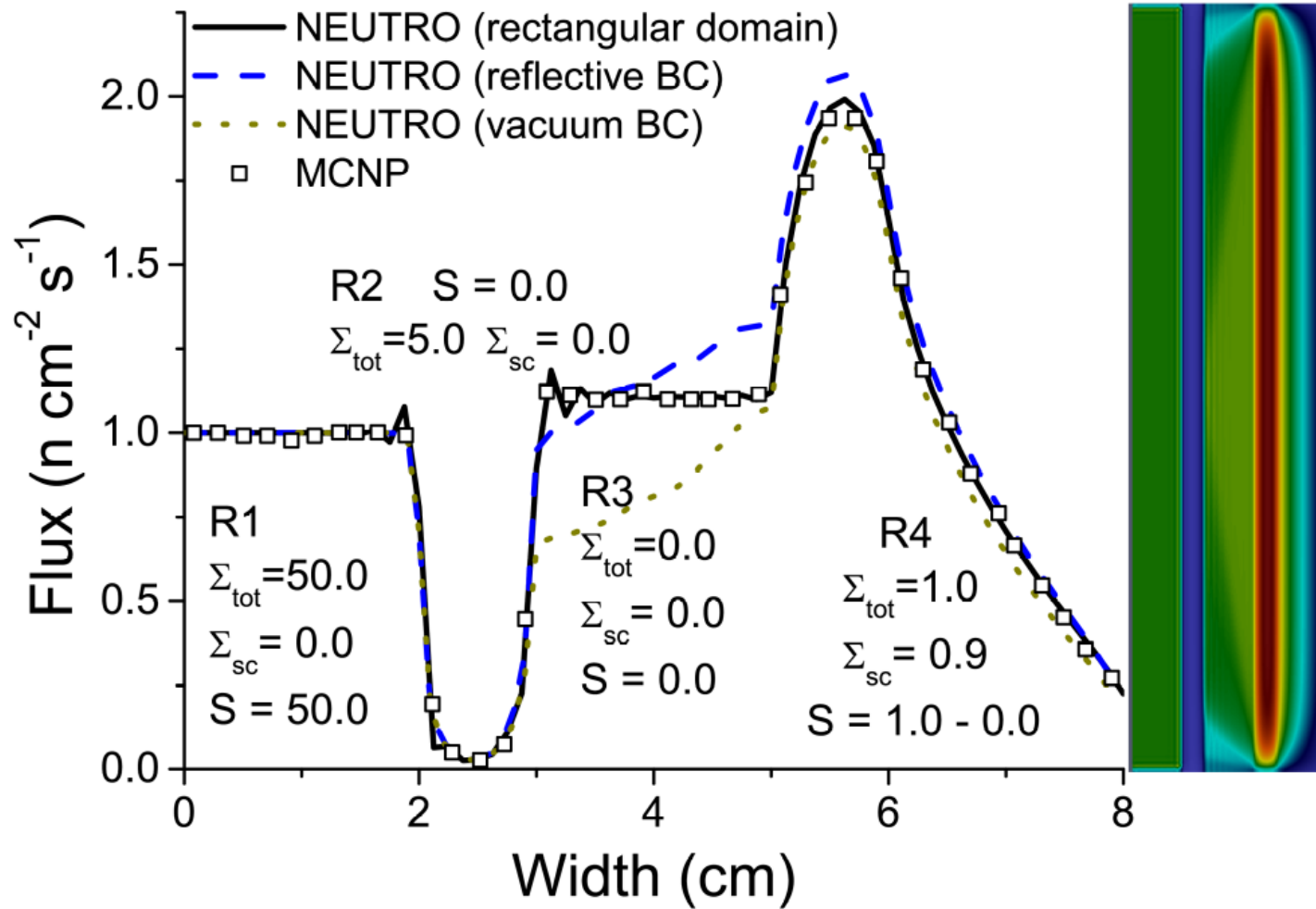
$$\sum_{g'=1}^G \sum_{m'=1}^M \sum_{l=0}^L \sum_{ml=-l}^l \frac{4\pi}{2l+1} Y_l^{ml}(\Omega_m) Y_l^{*ml}(\Omega_{m'}) \Sigma_{s_{mlg',gm',m}}(\mathbf{r}) \varphi_{g',m'}(\mathbf{r})$$

# NEUTRO: Present Status

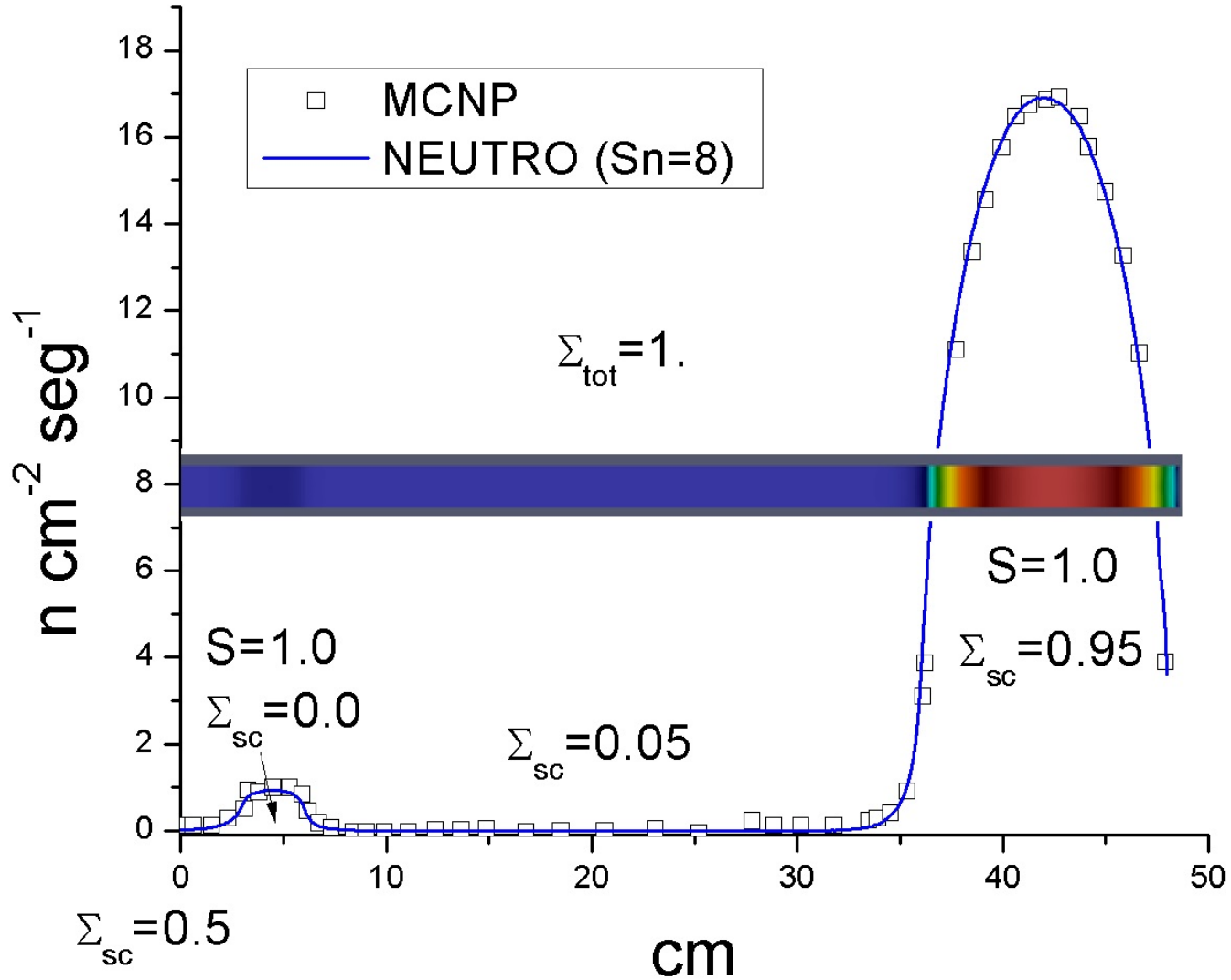
- ☀️ 3D domains with unstructured meshes.
- ☀️ Stationary simulations.
- ☀️ Anisotropic scattering.
- ☀️ Isotropic neutron source at boundaries.
- ☀️ Multiple heterogeneous materials.
- ☀️ Nuclear neutron-material heating.



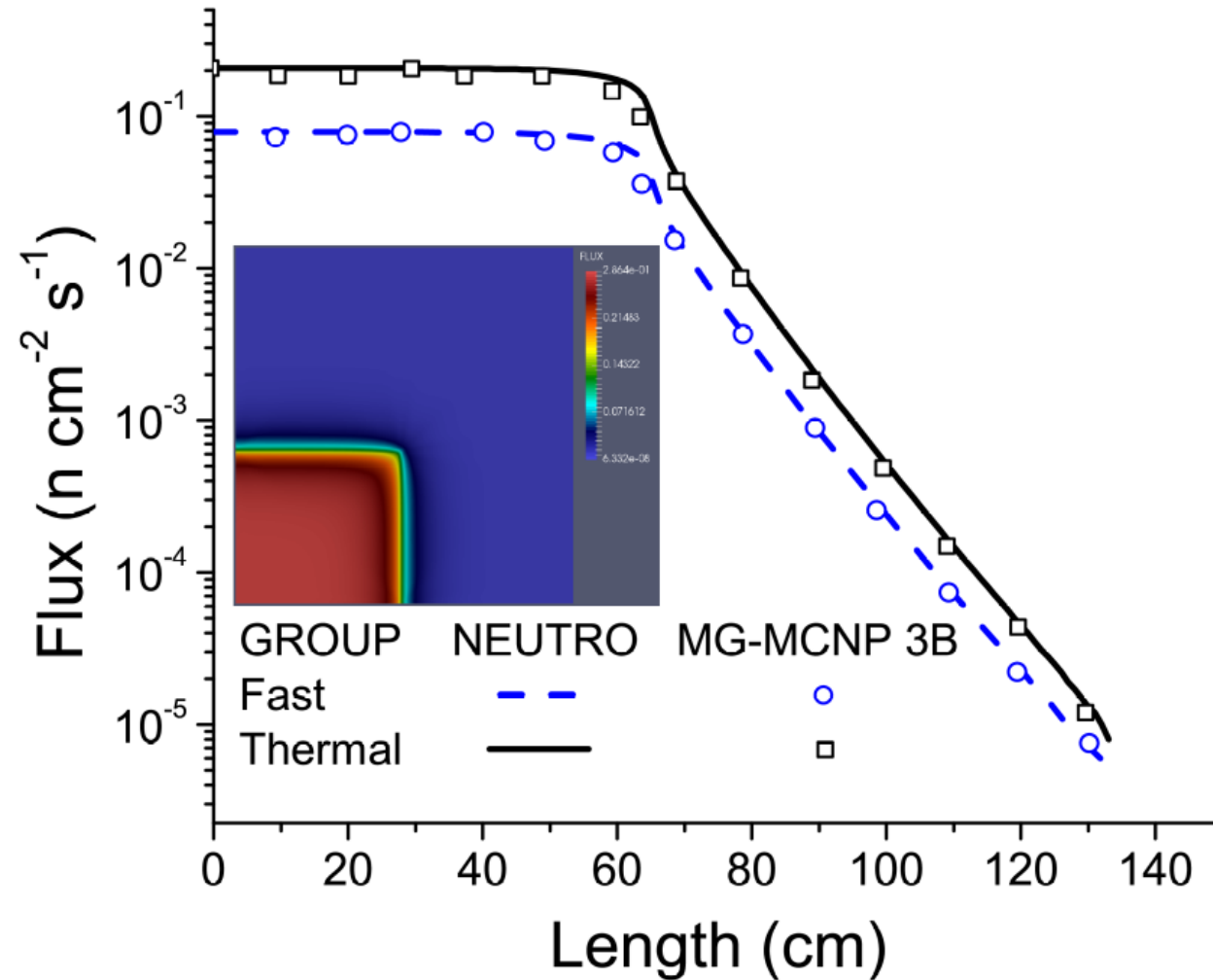
# Results: Reed test



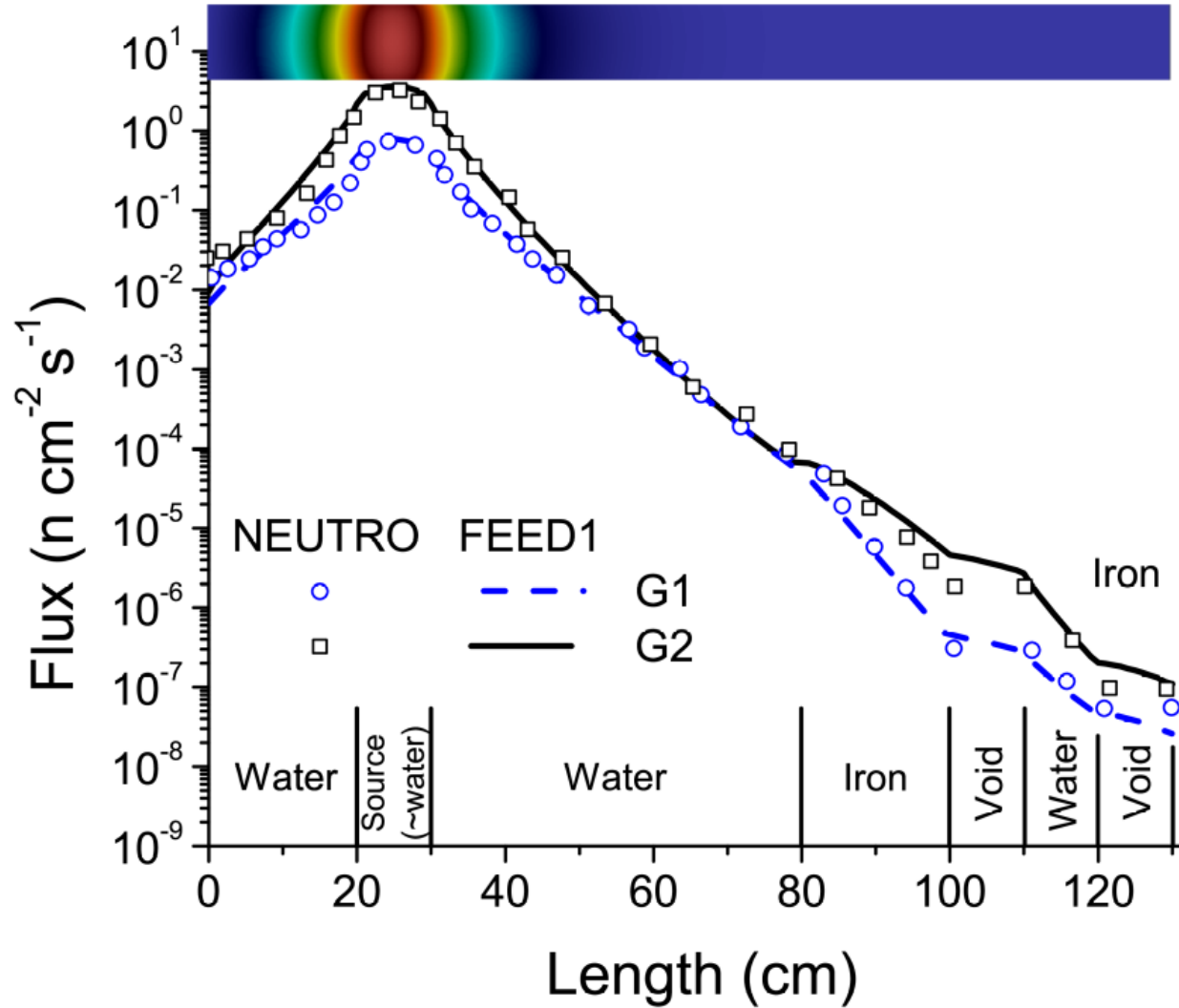
# Results: Alcouffe test



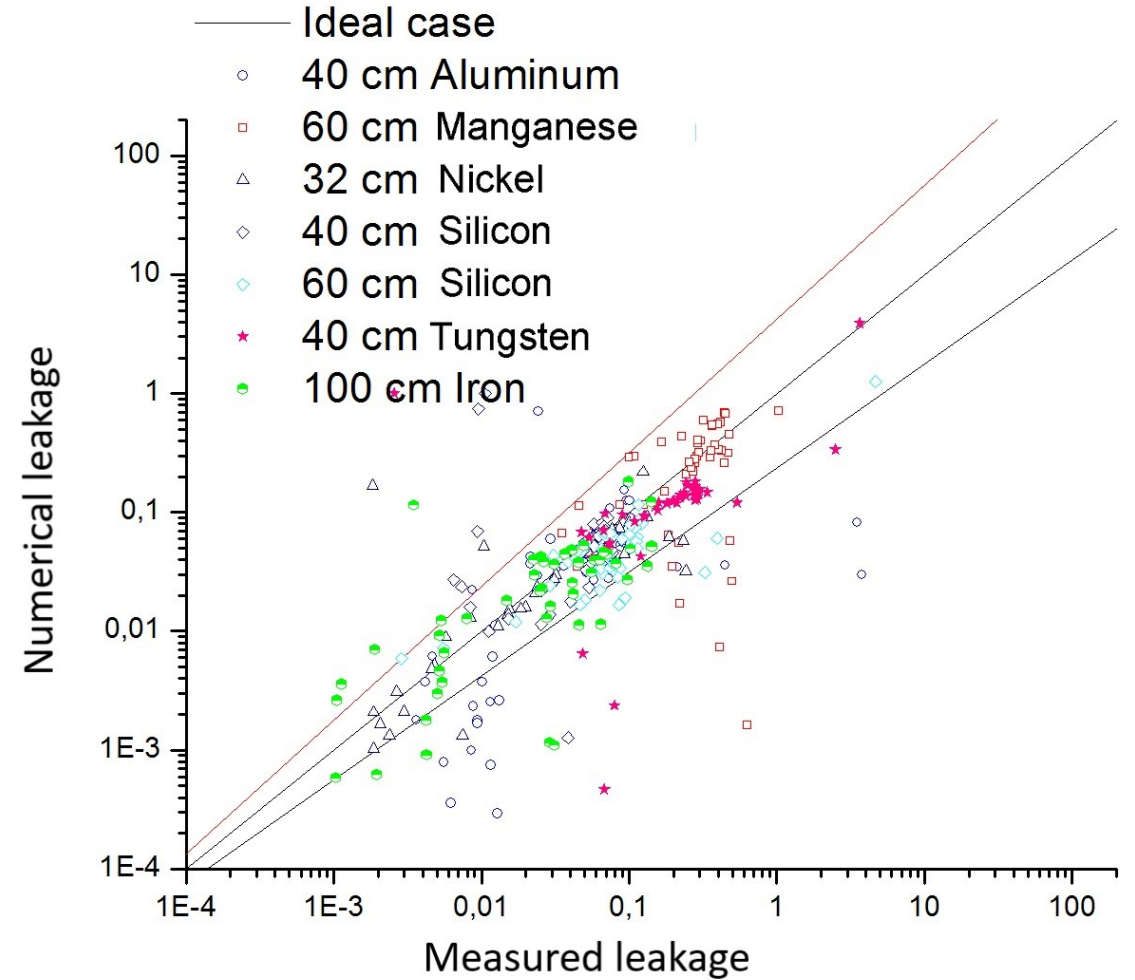
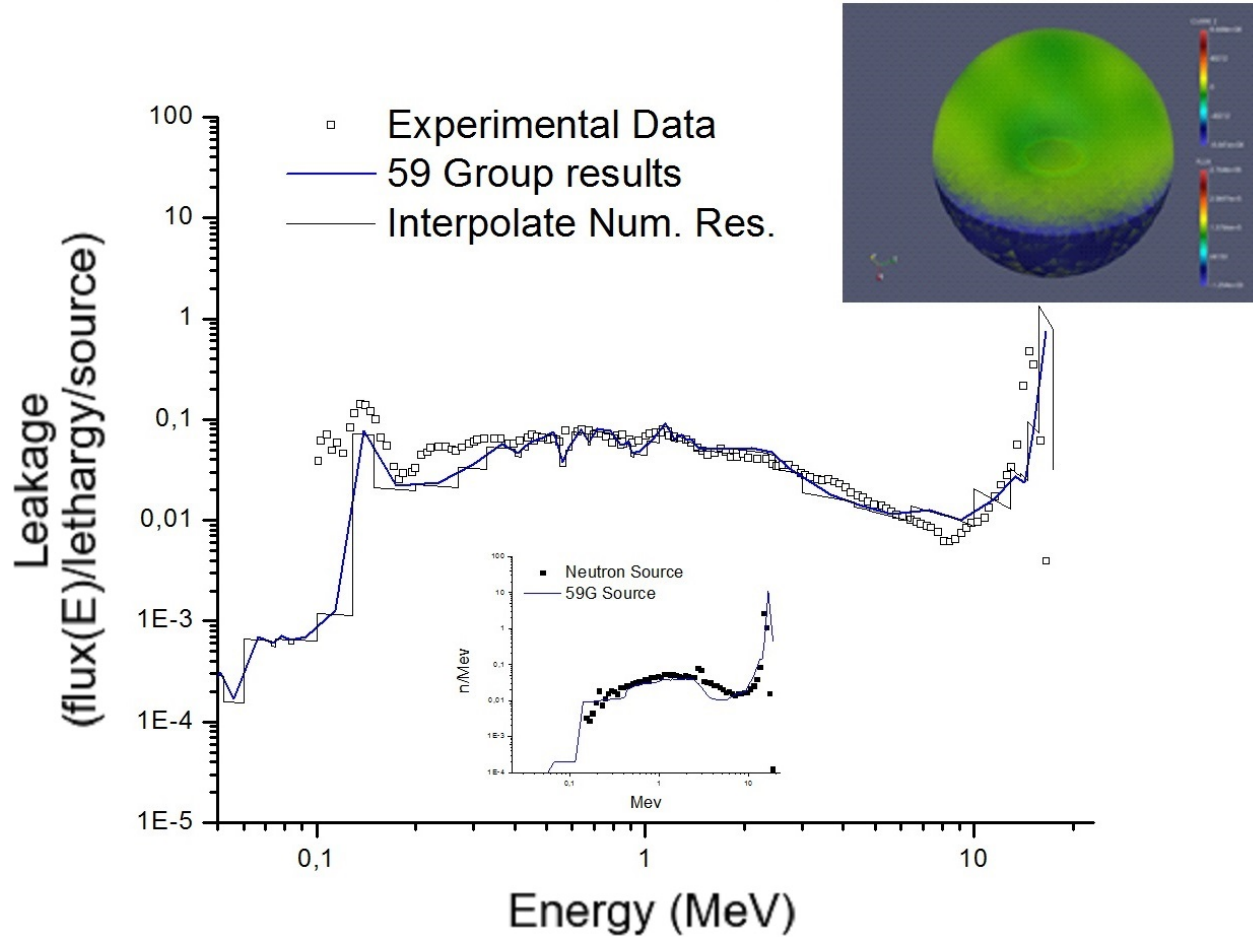
# Results: Deep penetration case



# Results: Shielding

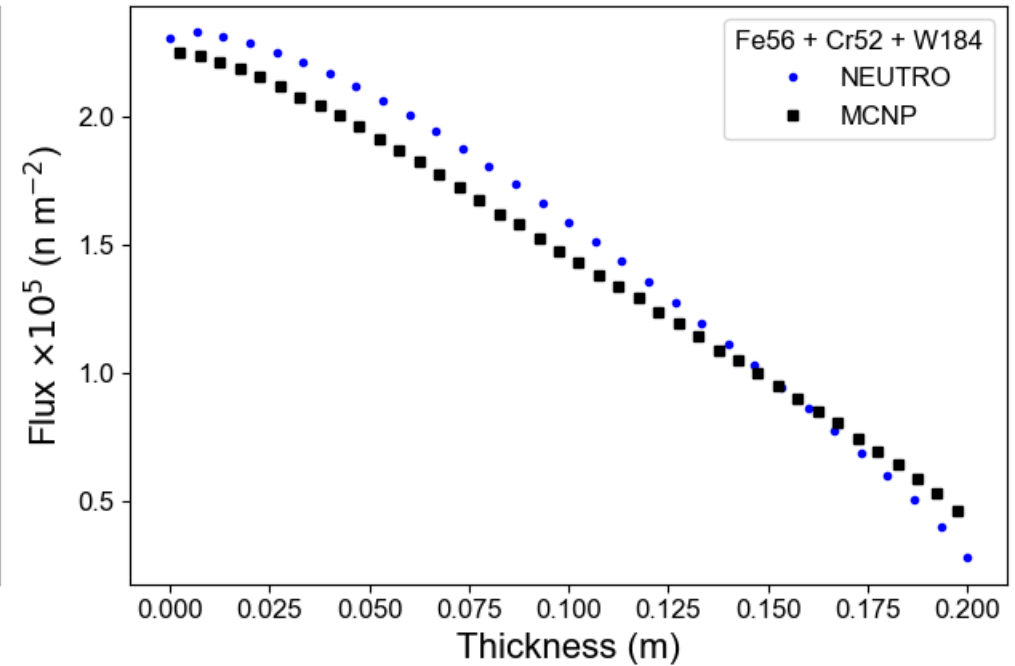
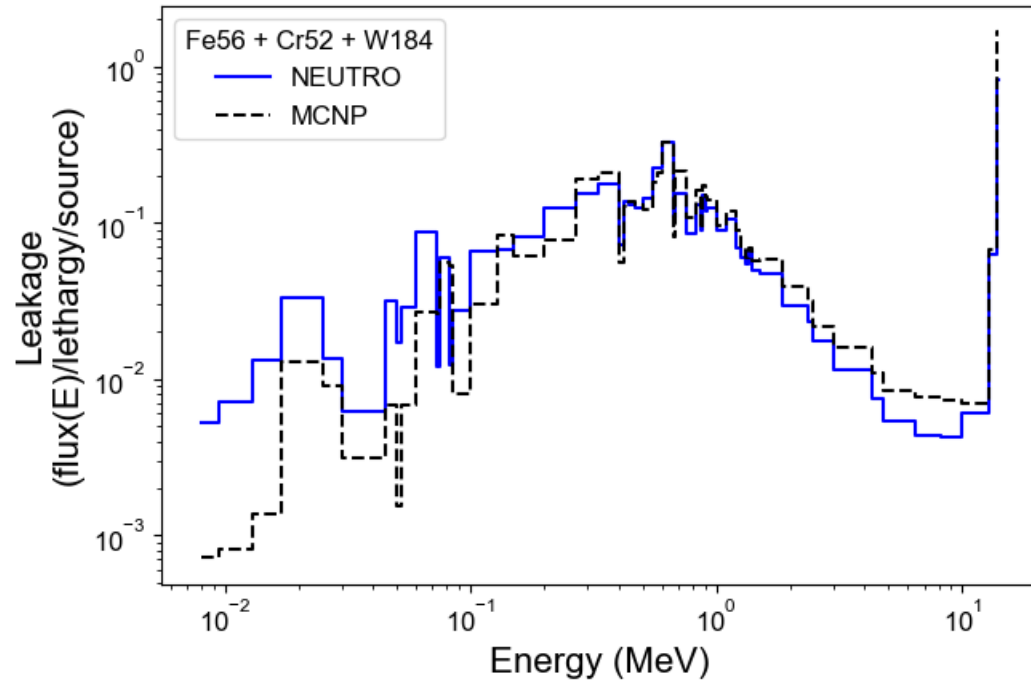


# Results: SINBAD testing





# Results: Comparing NEUTRO with MCNP

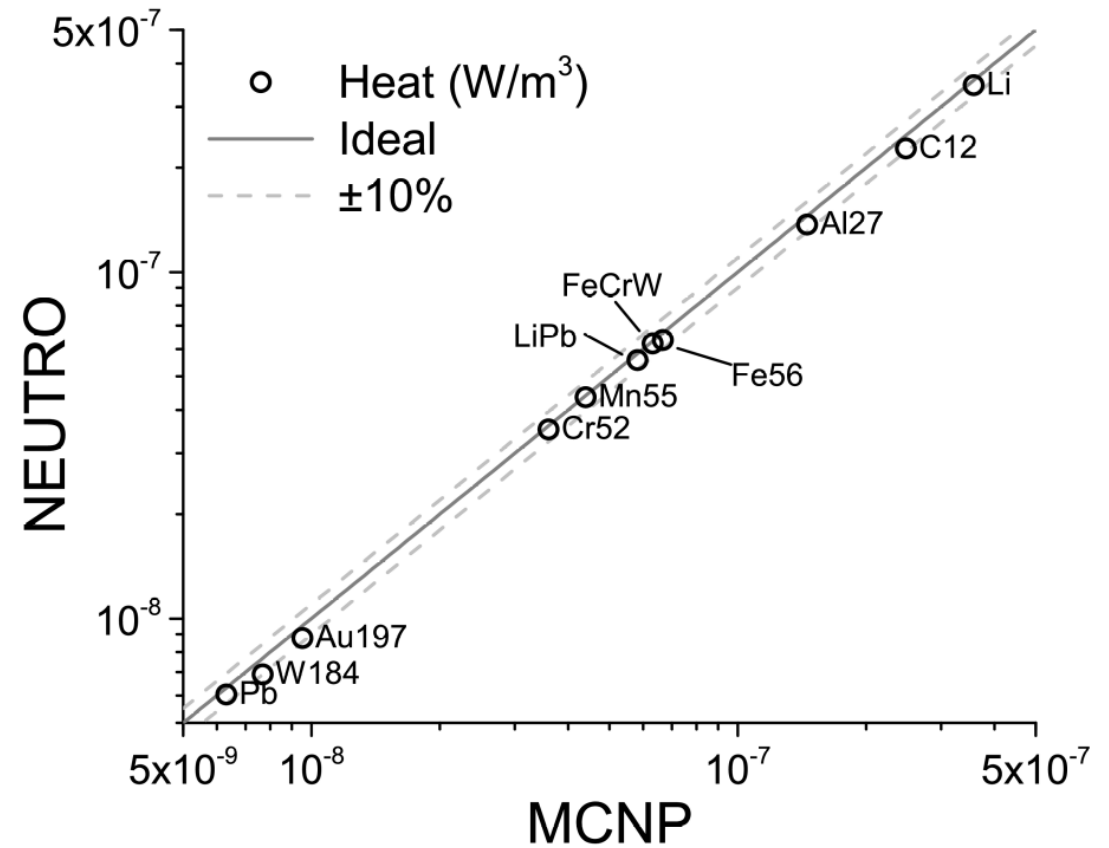


# Results: Comparing NEUTRO with MCNP

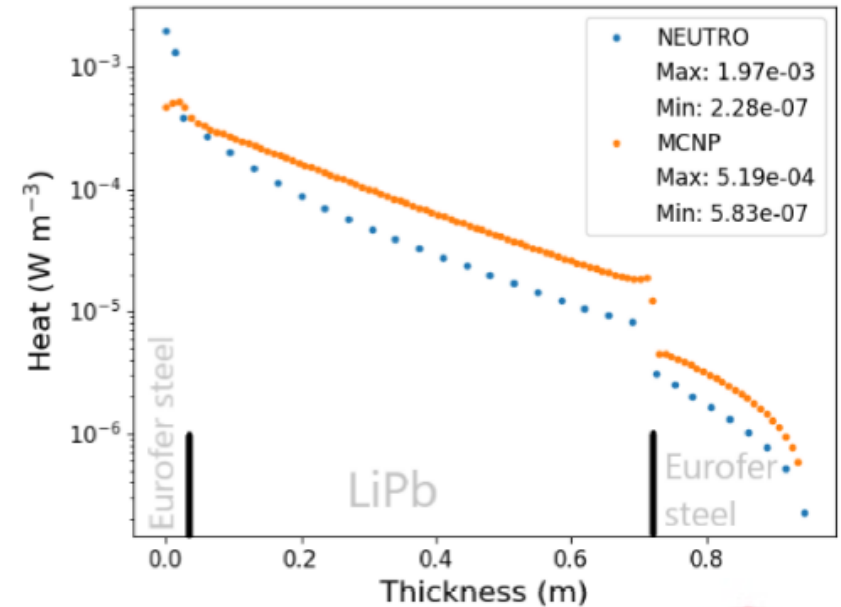
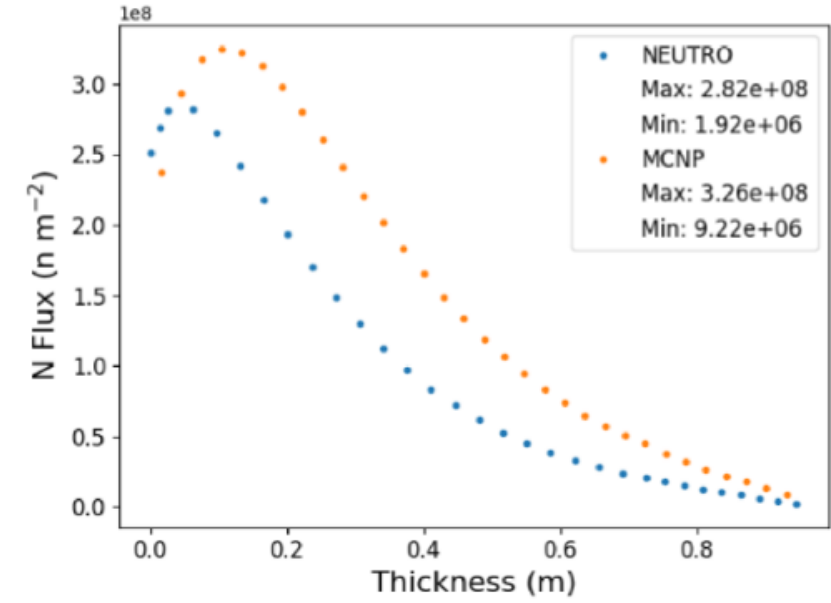
- ☀️ Include neutron heating:
  - ☀️ Neutron-material interaction.
  - ☀️ Photon-material interaction.
- ☀️ Heating is directly proportional to local neutron flux:

$$H(E) = \varphi(E) \cdot k(E)$$

where  $k(E) \equiv$  KERMA factor.

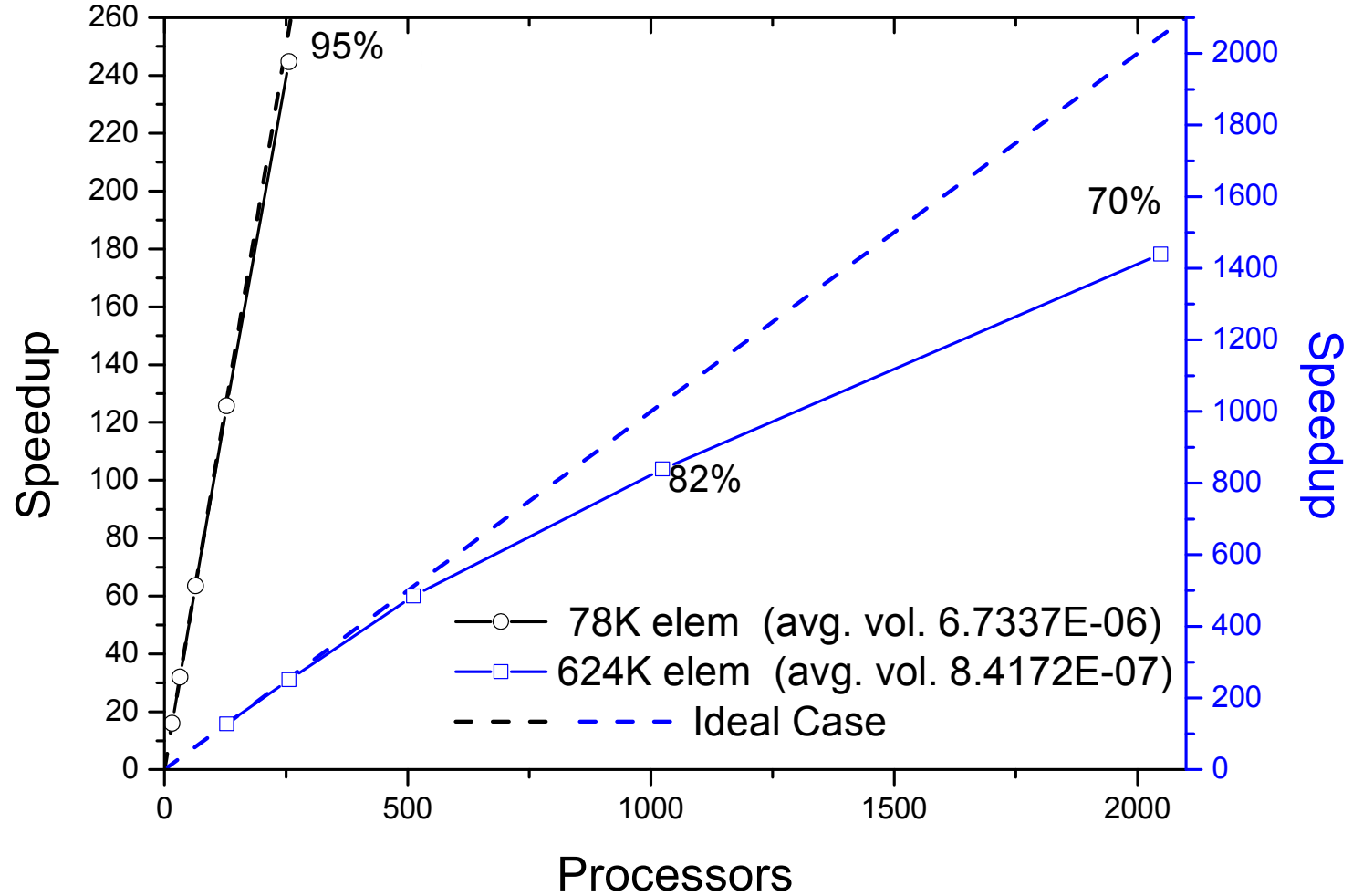
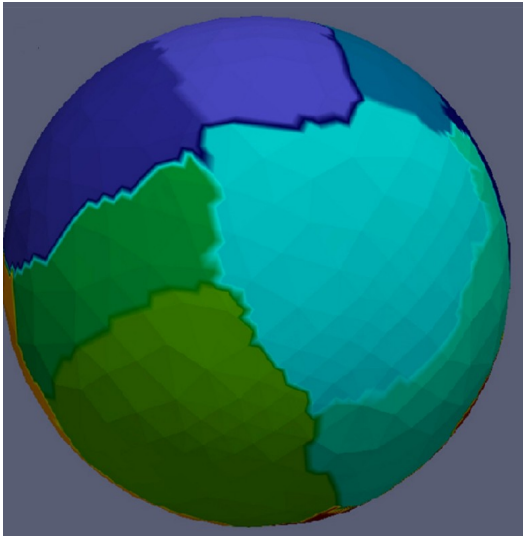


# Results: DEMO blanket



# HPC scalability

- Linear tetrahedral mesh
- Sn12 quadrature
- 59 energy groups



# Ongoing and future work

- ☀️ Calculate tritium production from neutron interaction with breeding blankets.
- ☀️ Further validation of heating due to neutron radiation interaction with materials.
- ☀️ Couple NEUTRO with other Alya modules and test validation cases solving multiphysics behaviour (thermal + mechanical + neutronics).

# Conclusions

- ☀️ Neutron transport code developed within Alya multiph,
- ☀️ Goal: a tool for contributing to reactor design studies.
- ☀️ Handle composite and alloy materials in 3D domains with unstructured meshes.
- ☀️ Tested against 4 classical tests.
- ☀️ Validations against 7 SINBAD experimental benchmark.
- ☀️ Heat due to neutron radiation interaction has been integrated in NEUTRO.
- ☀️ Compared NEUTRO against standard neutronics code.
- ☀️ Code scalability has been proved showing a nearly ideal behaviour up to 512 processors.
- ☀️ Expand code's features as a next step.



# Thank you for your attention



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